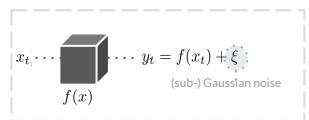
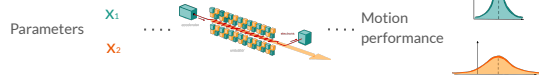


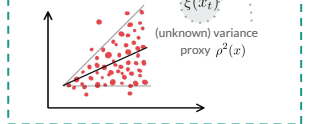
Black-box optimization arises in high-stakes applications



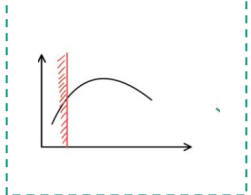
Tuning complex systems



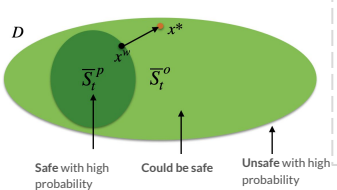
Problem 1: Two inputs x_1 and x_2 have similar expected output values, but one produces much noisier realizations



Problem 2: Input x_1 is safe and input x_2 is unsafe



2. Sketch GoOSE

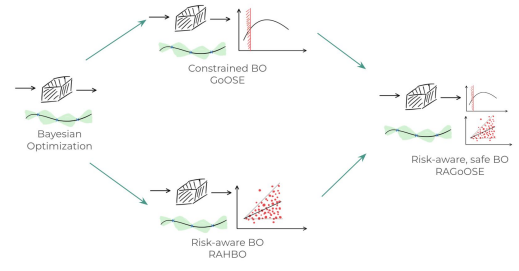


- for $t = 1, 2, \dots$
- choose action $x^* \in \bar{S}_t^o$
- if $x^* \in \bar{S}_t^p$: evaluate it and update \bar{S}_t^p and \bar{S}_t^o
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Takeaway

Practical optimization method that avoids choosing unsafe actions and takes into account unknown heteroscedastic noise.

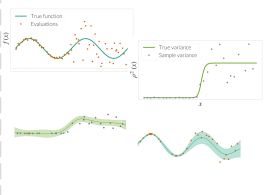
The RaGoose Algorithm



1. Sketch RAHBO

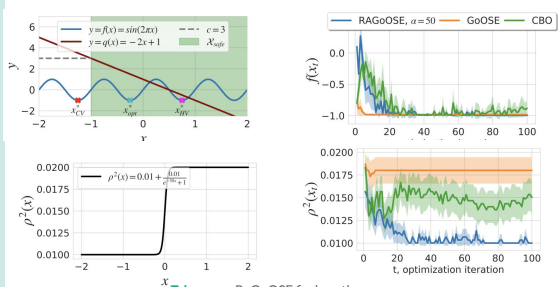
- Challenge 1: confidence bounds for $f(x)$ rely on known $\rho^2(x)$
- Challenge 2: estimate noise variance proxy $\rho^2(x)$.
- use conservative estimate to build $\operatorname{ucb}_t^{\text{RAHBO}}(x)$
 - repeat experiment k times to get sample variance

- for $t = 1, 2, \dots$
- choose $x_t \in \operatorname{argmax}_{x \in \mathcal{X}} \operatorname{ucb}_{t-1}^{\text{RAHBO}}(x) - \alpha \operatorname{lc}b_{t-1}^{\text{RAHBO}}(x)$
- collect k evaluations $\{y_i(x_t)\}_{i=1}^k$
- use sample mean and variance of $\{y_i(x_t)\}$ for GP posteriors
- update conf. bounds $\operatorname{lc}b_t^{\text{RAHBO}}(x)$ and $\operatorname{ucb}_t^{\text{RAHBO}}(x)$ for $\rho^2(x)$
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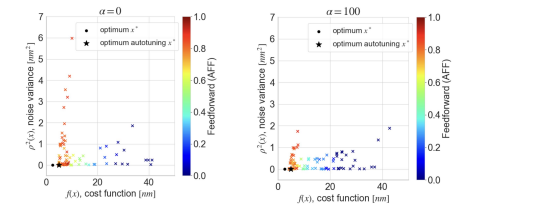
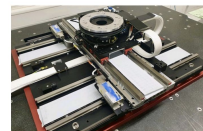
Experimental results

1. Synthetic experiment: sin function with three optima and sigmoid noise



Takeaway: RaGoOSE finds optimum with lower observation noise.

2. Real system: linear axis of a high precision positioning system



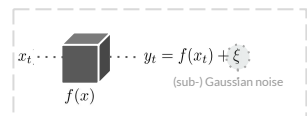
References

- Risk-averse heteroscedastic bayesian optimization; Makarova et al; Neurips 2021
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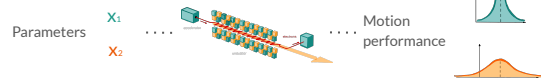
Paper:



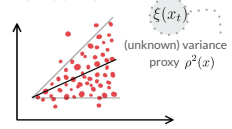
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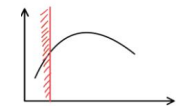
Tuning complex systems



Problem 1: Two inputs x_1 and x_2 have similar expected output values, but one produces much noisier realizations



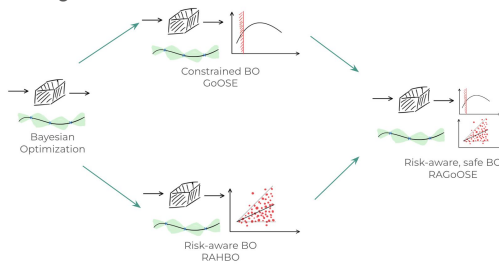
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The RaGoose Algorithm

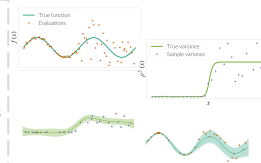


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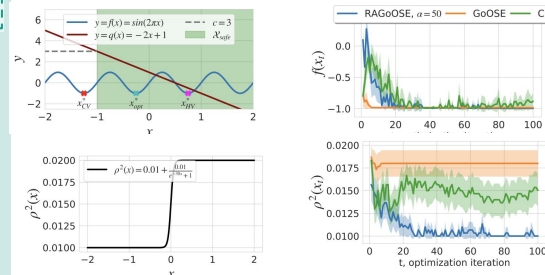
solutions

- for $t = 1, 2, \dots$
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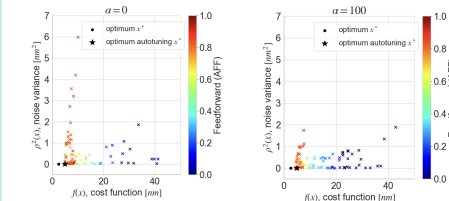
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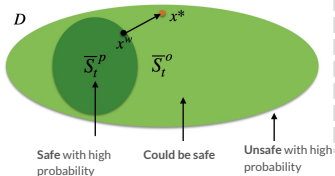
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Paper:



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